



25. Figure 1 shows a tile in the form of a trapezium, where $\alpha = 83\frac{1}{3}^{\circ}$. Several copies of the tile are placed together to form a symmetrical pattern, part of which is shown in Figure 2. The outer border of the complete pattern is a regular 'star polygon'. Figure 3 shows an example of a regular 'star polygon'.

Figure 1

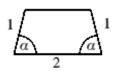


Figure 2



Figure 3



How many tiles are there in the complete pattern?

- A 48
- B 54
- C 60
- D 66
- E 72

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25. B Let the supplementary angle to α be β . Let tile 1 on the outside of the star polygon be horizontal. Counting anticlockwise around the star polygon, tile 3 has an angle of elevation from the horizontal of $\beta - \alpha = 96\frac{2}{3}^{\circ} - 83\frac{1}{3}^{\circ} = 13\frac{1}{3}^{\circ}$. As $360^{\circ} \div 13\frac{1}{3}^{\circ} = 27$, we need 27 pairs of tiles to complete one revolution. So there

are 54 tiles in the complete pattern.

