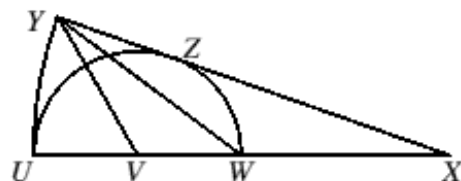




22. A semicircle of radius r is drawn with centre V and diameter UW . The line UW is then extended to the point X , such that UW and WX are of equal length. An arc of the circle with centre X and radius $4r$ is then drawn so that the line XY is a tangent to the



semicircle at Z , as shown. What, in terms of r , is the area of triangle YVW ?

- A $\frac{4r^2}{9}$ B $\frac{2r^2}{3}$ C r^2 D $\frac{4r^2}{3}$ E $2r^2$

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22. **B** Let the perpendicular from Y meet UV at T and let $\angle ZXV = \alpha$. Note that $\angle VZX = 90^\circ$ as a tangent to a circle is perpendicular to the radius at the point of contact. Therefore $\sin \alpha = \frac{r}{4r} = \frac{1}{4}$. Consider triangle YTX : $\sin \alpha = \frac{YT}{YX}$. So $YT = YX \sin \alpha = \frac{4r}{3}$. So the area of triangle $YVW = \frac{1}{2} \times VW \times YT = \frac{1}{2} \times r \times \frac{4r}{3} = \frac{2r^2}{3}$.

