



17. The two triangles have equal areas and the four marked lengths are equal. What is the value of  $x$ ?



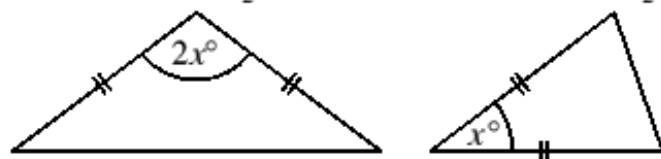
- A 30      B 45      C 60      D 75      E more information needed

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17. C Let the equal sides have length  $k$ . The height of the triangle on the left is  $k \cos x^\circ$  and its base is  $2k \sin x^\circ$ , so its area is  $k^2 \sin x^\circ \cos x^\circ$ . The height of the triangle on the right is  $k \sin x^\circ$  and its base is  $k$ , so its area is  $\frac{1}{2}k^2 \sin x^\circ$ . Hence  $\cos x^\circ = \frac{1}{2}$  and so  $x = 60$ .



(Alternatively, the formula  $\Delta = \frac{1}{2}ab \sin C$  can be used to show that  $\sin x^\circ = \sin 2x^\circ$ ; hence  $x + 2x = 180$ .)