

**MATHEMATICS**  
**Unit Statistics 3**

**MS03**

Friday 19 June 2009 1.30 pm to 3.00 pm

**For this paper you must have:**

- an 8-page answer book
  - the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

Time allowed: 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MS03.
- Answer **all** questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of tables or calculators should normally be given to three significant figures.

**Information**

- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

Answer **all** questions.

- 1 An analysis of a random sample of 150 urban dwellings for sale showed that 102 are semi-detached.

An analysis of an independent random sample of 80 rural dwellings for sale showed that 36 are semi-detached.

- (a) Construct an approximate 99% confidence interval for the difference between the proportion of urban dwellings for sale that are semi-detached and the proportion of rural dwellings for sale that are semi-detached. *(6 marks)*
- (b) Hence comment on the claim that there is no difference between these two proportions. *(2 marks)*

- 2 A hotel chain has hotels in three types of location: city, coastal and country. The percentages of the chain's reservations for each of these locations are 30, 55 and 15 respectively.

Each of the chain's hotels offers three types of reservation: Bed & Breakfast, Half Board and Full Board.

The percentages of these types of reservation for **each** of the three types of location are shown in the table.

		Type of location		
		City	Coastal	Country
Type of reservation	Bed & Breakfast	80	10	30
	Half Board	15	65	50
	Full Board	5	25	20

For example, 80 per cent of reservations for hotels in city locations are for Bed & Breakfast.

- (a) For a reservation selected at random:
- (i) show that the probability that it is for Bed & Breakfast is 0.34; *(2 marks)*
- (ii) calculate the probability that it is for Half Board in a hotel in a coastal location; *(2 marks)*
- (iii) calculate the probability that it is for a hotel in a coastal location, given that it is for Half Board. *(4 marks)*
- (b) A random sample of 3 reservations for Half Board is selected.

Calculate the probability that these 3 reservations are for hotels in different types of location. *(5 marks)*

- 3 The proportion,  $p$ , of an island's population with blood type A Rh<sup>+</sup> is believed to be approximately 0.35.

A medical organisation, requiring a more accurate estimate, specifies that a 98% confidence interval for  $p$  should have a width of at most 0.1.

Calculate, to the nearest 10, an estimate of the minimum sample size necessary in order to achieve the organisation's requirement. (6 marks)

- 4 Holly, a horticultural researcher, believes that the mean height of stems on Tahiti daffodils exceeds that on Jetfire daffodils by more than 15 cm.

She measures the heights,  $x$  centimetres, of stems on a random sample of 65 Tahiti daffodils and finds that their mean,  $\bar{x}$ , is 40.7 and that their standard deviation,  $s_x$ , is 3.4.

She also measures the heights,  $y$  centimetres, of stems on a random sample of 75 Jetfire daffodils and finds that their mean,  $\bar{y}$ , is 24.4 and that their standard deviation,  $s_y$ , is 2.8.

Investigate, at the 1% level of significance, Holly's belief. (8 marks)

- 5 The random variable  $X$  has a binomial distribution with parameters  $n$  and  $p$ .

- (a) Given that

$$E(X) = np \quad \text{and} \quad E(X(X - 1)) = n(n - 1)p^2$$

find an expression for  $\text{Var}(X)$ . (3 marks)

- (b) Given that  $X$  has a mean of 36 and a standard deviation of 4.8:

(i) find values for  $n$  and  $p$ ; (3 marks)

(ii) use a distributional approximation to estimate  $P(30 < X < 40)$ . (4 marks)

- 6 The table shows the probability distribution for the number of weekday (Monday to Friday) morning newspapers,  $X$ , purchased by the Reed household per week.

$x$	0	1	2	3	4	5
$P(X=x)$	0.16	0.15	0.25	0.25	0.15	0.04

- (a) Find values for  $E(X)$  and  $\text{Var}(X)$ . *(3 marks)*
- (b) The number of weekday (Monday to Friday) evening newspapers,  $Y$ , purchased by the same household per week is such that

$$E(Y) = 2.0, \quad \text{Var}(Y) = 1.5 \quad \text{and} \quad \text{Cov}(X, Y) = -0.43$$

Find values for the mean and variance of:

- (i)  $S = X + Y$ ;
- (ii)  $D = X - Y$ . *(5 marks)*
- (c) The total cost per week,  $L$ , of the Reed household's weekday morning and evening newspapers may be assumed to be normally distributed with a mean of £2.31 and a standard deviation of £0.89.

The total cost per week,  $M$ , of the household's weekend (Saturday and Sunday) newspapers may be assumed to be independent of  $L$  and normally distributed with a mean of £2.04 and a standard deviation of £0.43.

Determine the probability that the total cost per week of the Reed household's newspapers is more than £5. *(5 marks)*

7 The daily number of customers visiting a small arts and crafts shop may be modelled by a Poisson distribution with a mean of 24.

- (a) Using a distributional approximation, estimate the probability that there was a total of at most 150 customers visiting the shop during a given 6-day period. *(5 marks)*
- (b) The shop offers a picture framing service. The daily number of requests,  $Y$ , for this service may be assumed to have a Poisson distribution.

Prior to the shop advertising this service in the local free newspaper, the mean value of  $Y$  was 2. Following the advertisement, the shop received a total of 17 requests for the service during a period of 5 days.

- (i) Using a Poisson distribution, carry out a test, at the 10% level of significance, to investigate the claim that the advertisement increased the mean daily number of requests for the shop's picture framing service. *(5 marks)*
- (ii) Determine the critical value of  $Y$  for your test in part (b)(i). *(3 marks)*
- (iii) Hence, assuming that the advertisement increased the mean value of  $Y$  to 3, determine the power of your test in part (b)(i). *(4 marks)*

**END OF QUESTIONS**

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