



A-LEVEL Mathematics

MD02 – Decision 2

Mark scheme

6360

June 2018

Version/Stage: 1.0 Final



Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√ or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
-x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q1	Solution	Mark	Total	Comment																									
(a)	<table border="1"> <tr><td>6</td><td>11</td><td>7</td><td>2</td><td>**</td></tr> <tr><td>10</td><td>6</td><td>1</td><td>0</td><td>**</td></tr> <tr><td>9</td><td>8</td><td>6</td><td>8</td><td>**</td></tr> <tr><td>5</td><td>7</td><td>2</td><td>10</td><td>**</td></tr> <tr><td>8</td><td>10</td><td>5</td><td>5</td><td>**</td></tr> </table>	6	11	7	2	**	10	6	1	0	**	9	8	6	8	**	5	7	2	10	**	8	10	5	5	**	B1	2	All elements x replaced with $k - x$, $k \geq 19$
	6	11	7	2	**																								
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1	5	6	2	0																									
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0	4	5	1	0																									
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0*	3	4	0	0																									
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3	0*	3	6	0																									
0	0	0*	9	1																									
2	2	2	3	0*																									
	Five lines needed to cover the zeros, so optimal allocation found	A1	All correct with three lines drawn to cover zeros																										
	Tom will not be selected for the team OE	A1	Augmenting (by 1) with 4 or more rows/columns correct																										
		A1	All correct with five lines drawn to cover zeros and 'optimal' seen																										
		A1	CSO																										
	Total		9																										
<p>Notes: Candidate may write answer to (a) in (b), do not penalise, give benefit of doubt to candidate (b) need to see (at least) 'optimal' for A1 Statement about Tom needs to be in context, not just 'Tom'</p>																													

Q1	Solution	Mark	Total	Comment																									
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	<table border="1"> <tr><td>1</td><td>5</td><td>6</td><td>2</td><td>0</td></tr> <tr><td>5</td><td>0</td><td>0</td><td>0</td><td>0</td></tr> <tr><td>4</td><td>2</td><td>5</td><td>8</td><td>0</td></tr> <tr><td>0</td><td>1</td><td>1</td><td>10</td><td>0</td></tr> <tr><td>3</td><td>4</td><td>4</td><td>5</td><td>0</td></tr> </table>	1	5	6	2	0	5	0	0	0	0	4	2	5	8	0	0	1	1	10	0	3	4	4	5	0	M1		Column reduction with 4 or more columns correct
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	Five lines needed to cover the zeros, so optimal allocation found	A1		All correct with five lines drawn to cover zeros and 'optimal' seen																									
	Tom will not be selected for the team	A1	7	CSO																									
	Total		9																										

Q2	Solution	Mark	Total	Comment																																													
(a) (i)	$[18 + 20 + 25 + 87] = 150$	B1																																															
(a) (ii)	$[51 + 14 - 5 - 3 + 87] = 144$	B1	2																																														
(b)	[Max] flow \leq their min from (a)	M1																																															
	[Max] flow of gas [through the network of] pipes must be less than or equal to $144 \text{ cm}^3 \text{ s}^{-1}$ OE	A1	2	Including units																																													
(c)(i)	<table border="1"> <thead> <tr> <th>Arc</th> <th>Forward</th> <th>Backward</th> </tr> </thead> <tbody> <tr><td>SA</td><td>29</td><td>0</td></tr> <tr><td>AC</td><td>4</td><td>0</td></tr> <tr><td>CF</td><td>17</td><td>5</td></tr> <tr><td>FT</td><td>68</td><td>0</td></tr> <tr><td>AD</td><td>1</td><td>6</td></tr> <tr><td>DF</td><td>6</td><td>5</td></tr> <tr><td>DC</td><td>15</td><td>0</td></tr> <tr><td>DE</td><td>8</td><td>0</td></tr> <tr><td>SB</td><td>32</td><td>0</td></tr> <tr><td>BE</td><td>14</td><td>3</td></tr> <tr><td>EG</td><td>4</td><td>10</td></tr> <tr><td>GT</td><td>67</td><td>0</td></tr> <tr><td>BD</td><td>0</td><td>4</td></tr> <tr><td>DG</td><td>22</td><td>2</td></tr> </tbody> </table>	Arc	Forward	Backward	SA	29	0	AC	4	0	CF	17	5	FT	68	0	AD	1	6	DF	6	5	DC	15	0	DE	8	0	SB	32	0	BE	14	3	EG	4	10	GT	67	0	BD	0	4	DG	22	2	M1		Correct at SA, AC, SB, and BE
Arc	Forward	Backward																																															
SA	29	0																																															
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EG	4	10																																															
GT	67	0																																															
BD	0	4																																															
DG	22	2																																															
		M1		Correct at CF, FT, EG, and GT																																													
		A1	3	All correct																																													
(c)(ii)	Modifying one feasible flow (both increasing and decreasing) correctly on the diagram	B1																																															
	e.g.	M1		One correct path and extra flow in table																																													
	<table border="1"> <thead> <tr> <th>Path</th> <th>Extra Flow</th> </tr> </thead> <tbody> <tr><td>SACFT</td><td>4</td></tr> <tr><td>SAD(CF, F or G)T</td><td>1</td></tr> <tr><td>SBEGT</td><td>4</td></tr> </tbody> </table>	Path	Extra Flow	SACFT	4	SAD(CF, F or G)T	1	SBEGT	4	A1		Two correct paths and extra flows in table																																					
Path	Extra Flow																																																
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SBEGT	4																																																
		A1	4	All correct																																													
(c)(iii)	[Max. flow = $38 + 4 + 1 + 4 =$] $47 \text{ [cm}^3 \text{ s}^{-1}]$	B1	1																																														
	Total		12																																														

Notes: (b) may see symbols for 'less than or equal to'

(c) If **M0** scored in (i), then candidate scores **B0** in (ii)

(c)(i) if **M0M0** scored, **SC1** for SA, AC, CF, FT or SB, BE, EG, GT all correct

(c)(ii) there are other obtuse possibilities, but any correct soln must have total(SA...T) = 5 and SBEGT = 4

Note: there is no path SACD..T allowable

Q3	Solution	Mark	Total	Comment								
(a)	Use of p and $1 - p$ for John's strategies	M1										
	<table border="1"> <thead> <tr> <th>[If Winnie plays]</th> <th>[Expected gain for John]</th> </tr> </thead> <tbody> <tr> <td>[W₁]</td> <td>$0p + (-2)(1 - p) [= 2p - 2]$</td> </tr> <tr> <td>[W₂]</td> <td>$-2p + 7(1 - p) [= 7 - 9p]$</td> </tr> <tr> <td>[W₃]</td> <td>$4p + (-6)(1 - p) [= 10p - 6]$</td> </tr> </tbody> </table>	[If Winnie plays]	[Expected gain for John]	[W ₁]	$0p + (-2)(1 - p) [= 2p - 2]$	[W ₂]	$-2p + 7(1 - p) [= 7 - 9p]$	[W ₃]	$4p + (-6)(1 - p) [= 10p - 6]$	A1		One correct expression
[If Winnie plays]	[Expected gain for John]											
[W ₁]	$0p + (-2)(1 - p) [= 2p - 2]$											
[W ₂]	$-2p + 7(1 - p) [= 7 - 9p]$											
[W ₃]	$4p + (-6)(1 - p) [= 10p - 6]$											
		A1		All three expressions correct								
		M1		Three lines								
		A1		All three ruled lines correct (-2 to 0, 7 to -2 and -6 to 4) with numbers on both vertical axes								
	[Optimal/maximum at] $2p - 2 = 7 - 9p$	A1										
	$[p = 9/11]$											
	[Value of the game for John]: $[2 \times (9/11) - 2] = -4/11$ OE	A1	7	Must be exact								

(b)	<table border="1"> <thead> <tr> <th>[If John plays]</th> <th>[Expected gain for Winnie]</th> </tr> </thead> <tbody> <tr> <td>[J₁]</td> <td>$0q + (-2)r + 4(1 - q - r) [= 4 - 4q - 6r]$</td> </tr> <tr> <td>[J₂]</td> <td>$-2q + 7r + (-6)(1 - q - r) [= -6 + 4q + 13r]$</td> </tr> </tbody> </table>	[If John plays]	[Expected gain for Winnie]	[J ₁]	$0q + (-2)r + 4(1 - q - r) [= 4 - 4q - 6r]$	[J ₂]	$-2q + 7r + (-6)(1 - q - r) [= -6 + 4q + 13r]$	M1		Either expression correct (including the use of exactly two probability variables)
	[If John plays]	[Expected gain for Winnie]								
[J ₁]	$0q + (-2)r + 4(1 - q - r) [= 4 - 4q - 6r]$									
[J ₂]	$-2q + 7r + (-6)(1 - q - r) [= -6 + 4q + 13r]$									
$4 - 4q - 6r = -4 / 11$ $-6 + 4q + 13r = -4 / 11$		A1F		Sets the correct expressions equal to their value of the game from (b)						
$q = 9/11, r = 2/11$		A1		Both values correct						
Winnie plays: W₁ [with probability] 9/11 W₂ [with probability] 2/11 W₃ [with probability] 0		E1	4	Must have all three probabilities						
Alternative Solution Winnie never plays W₃ so										
<table border="1"> <thead> <tr> <th>[If John plays]</th> <th>[Expected gain for Winnie]</th> </tr> </thead> <tbody> <tr> <td>[J₁]</td> <td>$0p + (-2)(1 - p) [= -2 + 2p]$</td> </tr> <tr> <td>[J₂]</td> <td>$-2p + 7(1 - p) [= 7 - 9p]$</td> </tr> </tbody> </table>	[If John plays]	[Expected gain for Winnie]	[J ₁]	$0p + (-2)(1 - p) [= -2 + 2p]$	[J ₂]	$-2p + 7(1 - p) [= 7 - 9p]$		(M1)		Either expression correct
[If John plays]	[Expected gain for Winnie]									
[J ₁]	$0p + (-2)(1 - p) [= -2 + 2p]$									
[J ₂]	$-2p + 7(1 - p) [= 7 - 9p]$									
$-2 + 2p = 7 - 9p$		(A1)		Sets the correct gain expressions equal to each other						
$p = 9/11$		(A1)								
Winnie plays: W₁ [with probability] 9/11 W₂ [with probability] 2/11 W₃ [with probability] 0		(E1)		Must have all three probabilities, but W₃ may be stated as never played earlier in the solution						
	Total		11							
Notes: Marks for (a) may be earned in a candidate's solution to (b). Consult team leader (a) Each A mark is only dependent on the previous M mark eg M1A1A0 M1A0A1 ...										

Q4	Solution				Mark	Total	Comment
	Stage	State	From	Value			
	1	<i>I</i>	<i>T</i>	475*			
		<i>J</i>	<i>T</i>	480*			
		<i>K</i>	<i>T</i>	475*			
	2	<i>D</i>	<i>I</i>	max(470, 475)	B1		9 Values at Stage 2
		<i>E</i>	<i>I</i>	max(470, 475)			
			<i>J</i>	max(465, 480)			
		<i>F</i>	<i>I</i>	max(495, 475)	M1		Using minimax – choosing at least two of EI, FJ or GK (PI)
			<i>J</i>	max(490, 480)			
			<i>K</i>	max(495, 475)			
		<i>G</i>	<i>J</i>	max(485, 480)			
			<i>K</i>	max(480, 475)			
		<i>H</i>	<i>K</i>	max(475, 475)	A1		All values correct at Stage 2
	3	<i>A</i>	<i>D</i>	max(480, 475)			
			<i>E</i>	max(515, 475)			
			<i>F</i>	max(490, 490)	B1		9 Values at Stage 3
		<i>B</i>	<i>E</i>	max(485, 475)			
			<i>F</i>	max(475, 490)	dM1		At least 7 values correct
			<i>G</i>	max(480, 480)			
		<i>C</i>	<i>F</i>	max(490, 490)	A1		All values correct at Stage 3
			<i>G</i>	max(500, 480)			
			<i>H</i>	max(495, 475)			
	4	<i>S</i>	<i>A</i>	max(465, 480)	B1		3 Values at Stage 4
			<i>B</i>	max(470, 480)			
			<i>C</i>	max(460, 490)	A1		All values correct at Stage 4
	<i>S-B-G-K-T</i>				A1		One correct route (not reversed)
	<i>S-A-D-I-T</i>				A1		2 nd correct route (not reversed) AND no others
	[Longest Days Driving Time =] 480 minutes OE				B1	11	Must include units
	Total				11		
Notes: condone omission of max comparisons eg max(470, 475)							

Q5	Solution	Mark	Total	Comment																
(a)	$a < 0$	B1	1																	
(b)	$\frac{b}{1/2} < \frac{c}{3/2}$	M1																		
	$3b < c$	A1	2	NMS 2/2																
(c)(i)	$d \pm 3 \times 7/2$	M1																		
	$d + 21/2$ OE	A1	2	NMS 2/2																
(c)(ii)	<table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th><i>P</i></th> <th><i>x</i></th> <th><i>y</i></th> <th><i>z</i></th> <th><i>s</i></th> <th><i>t</i></th> <th><i>u</i></th> <th>value</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>0</td> <td>0</td> <td>$35 - 7a$</td> <td>$-2a$</td> <td>$10 + a$</td> <td>0</td> <td>$100 - 2ab$</td> </tr> </tbody> </table>	<i>P</i>	<i>x</i>	<i>y</i>	<i>z</i>	<i>s</i>	<i>t</i>	<i>u</i>	value	1	0	0	$35 - 7a$	$-2a$	$10 + a$	0	$100 - 2ab$	B1		$P = 1, x = 0, y = 0$ and $u = 0$ all correct
<i>P</i>	<i>x</i>	<i>y</i>	<i>z</i>	<i>s</i>	<i>t</i>	<i>u</i>	value													
1	0	0	$35 - 7a$	$-2a$	$10 + a$	0	$100 - 2ab$													
		M1		One of z, s or t correct																
		A1		z, s and t all correct																
		B1	4	value = $100 - 2ab$																
(c)(iii)	$10 + a \geq 0$ OE	M1		<i>their</i> $t \geq 0$ PI by final answer																
	$-10 \leq a < 0$	A1	2	Allow $-10 \leq a$ AND $a < 0$																
Total			11																	

Notes: (b) For **A1**, accept $b < \frac{1}{3}c$, or $\frac{1}{3}c > b$ or $c > 3b$ BUT NOT $6b < 2c$

(c)(i)(ii) for both parts condone correct multiples for all marks eg $d/k + 21/2k$

(ii) condone omission of 'heading row', but be convinced

(iii) *their* $(10 + a) \geq 0$ seen anywhere in soln scores **M1**

Q6	Solution	Mark	Total	Comment																																				
(a)	<table border="1"> <thead> <tr> <th>Activity</th> <th>Early</th> <th>Late</th> </tr> </thead> <tbody> <tr><td>A</td><td>0</td><td>7</td></tr> <tr><td>B</td><td>0</td><td>6</td></tr> <tr><td>C</td><td>5</td><td>15</td></tr> <tr><td>D</td><td>6</td><td>14</td></tr> <tr><td>E</td><td>6</td><td>14</td></tr> <tr><td>F</td><td>13</td><td>22</td></tr> <tr><td>G</td><td>14</td><td>22</td></tr> <tr><td>H</td><td>14</td><td>23</td></tr> <tr><td>I</td><td>22</td><td>31</td></tr> <tr><td>J</td><td>22</td><td>31</td></tr> <tr><td>K</td><td>31</td><td>40</td></tr> </tbody> </table>	Activity	Early	Late	A	0	7	B	0	6	C	5	15	D	6	14	E	6	14	F	13	22	G	14	22	H	14	23	I	22	31	J	22	31	K	31	40	B1	2	All early times correct
	Activity	Early	Late																																					
	A	0	7																																					
	B	0	6																																					
	C	5	15																																					
	D	6	14																																					
	E	6	14																																					
	F	13	22																																					
	G	14	22																																					
	H	14	23																																					
	I	22	31																																					
J	22	31																																						
K	31	40																																						
		B1	All late times correct																																					
(b)	B-E-G-I-K	B1	1	Or reverse																																				
(c)		M1	3	SCA, at least 10 labelled activities																																				
		B1		Use of floats, at least three of A, C, D, F, H, J (either before or after activity)																																				
		A1		All correct, including labelling and all floats before activity correct																																				
(d)(i)	Reduce G by 5 days Reduce both F and H by 3 days	E1 E1	5	Decrease G to 3 days Decrease F and H both to 4 days																																				
(d)(ii)	Cost of reducing to the minimum completion time $(g \times 500) + (f \times 250) + (h \times 650)$ (with at least 2 of their f, g, h non-zero)	M1		Calculates cost of reducing durations by 'their' reductions in (d)(i)																																				
	[£]5200 [£]5200 > [£]5000, (so the company will not make a profit from the bonus payment) so don't reduce (F, G, H)	A1 E1F		CAO Comparing their 5200 to 5000 PI and making a correct conclusion about whether to reduce durations																																				
	Total		11																																					
Notes: (c) For M1 all non-critical activities must be on a separate row (d)(ii) eg if their answer is less than 5000, (the company would benefit from the bonus) so reduce E1F Accept: 'Yes/No' plus valid reason in context																																								

Q7	Solution	Mark	Total	Comment	
(a)	Row Minima = $-2, -5, -6, -2$ Column Maxima = $-2, 6, -2, 7$	M1	4	Finds all row minima or all column maxima (may be seen on table.) Condone one slip	
	Max(Row Minima) = -2 Min(Row Maxima) = -2	A1		Both correct (may be indicated, not stated from 8 correct values)	
	Any two of AW, AY, DW and DY stated	A1			
	All four saddle points correct and no others stated	A1		AW, AY, DW and DY.	
	(b) Y dominates Z	B1	6	OE statement with $x < -3$ mentioned/used	
	as $\begin{pmatrix} 2x \\ x-3 \\ -2 \\ -2 \end{pmatrix} < \begin{pmatrix} 3 \\ -5 \\ 7 \\ 6 \end{pmatrix}$ for integer $x < -3$.	E1			
	D dominates C	B1 dep			Dependent on first B mark
	as $(x-1 \quad 1 \quad -2) \geq (x-3 \quad 3x-3 \quad -2)$ for integer $x < -3$.	E1			OE statement with $x < -3$ mentioned/used
	W (or Y) dominates X	B1 dep			Dependent on first and second B marks, and no other further dominances stated/used
	as $\begin{pmatrix} -2 \\ -3 \\ x-1 \end{pmatrix} < \begin{pmatrix} 5 \\ 6 \\ 1 \end{pmatrix}$ for integer $x < -3$	E1			OE statement with $x < -3$ mentioned/used
$\left[\text{or } \begin{pmatrix} 2x \\ x-3 \\ -2 \end{pmatrix} < \begin{pmatrix} 5 \\ 6 \\ 3 \end{pmatrix} \right]$					
Total			10		

Notes: **(a)** the final **A1A1** are independent of previous **A1**
 the 'co-ordinates eg AW' must be stated not merely circling entries in the table for the final **A1A1**
 If **M0** scored then **SC1** for two or more correct saddle points
(b) working may be seen on table
 A candidate may subst $x = -4$ (instead of $x < -3$) and consider dominance as above. In this case all marks are available. (possibly by drawing a new amended matrix)
 A candidate who subst $x = -3$ can score the **B** marks only