



9. A square has vertices at  $(0, 0)$ ,  $(1, 0)$ ,  $(1, 1)$  and  $(0, 1)$ . Graphs of the following equations are drawn on the same set of axes as the square.

$$x^2 + y^2 = 1, \quad y = x + 1, \quad y = -x^2 + 1, \quad y = x, \quad y = \frac{1}{x}$$

How many of the graphs pass through exactly two of the vertices of the square?

- A 1                      B 2                      C 3                      D 4                      E 5



9. C Let  $O = (0,0)$ ,  $A = (1,0)$ ,  $B = (1,1)$ ,  $C = (0,1)$  be the vertices of the square. The equation  $x^2 + y^2 = 1$  gives a circle passing through  $A$  and  $C$ . The equation  $y = x + 1$  gives a straight line passing only through  $C$ . The equation  $y = -x^2 + 1$  gives a parabola passing through  $A$  and  $C$ . The equation  $y = x$  gives a straight line passing through  $O$  and  $B$ . The equation  $y = \frac{1}{x}$  gives a rectangular hyperbola which has two branches and passes only through  $B$ . So, only  $x^2 + y^2 = 1$ ,  $y = x$  and  $y = -x^2 + 1$  have graphs passing through exactly two of the vertices of the square.

