



4. Alex draws a scalene triangle. One of the angles is  $80^\circ$ . Which of the following could be the difference between the other two angles in Alex's triangle?
- A  $0^\circ$                       B  $60^\circ$                       C  $80^\circ$                       D  $100^\circ$                       E  $120^\circ$

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4. C One angle in Alex's triangle is  $80^\circ$ . Let  $a^\circ$  be the smaller of the other two angles so  $(100 - a)^\circ$  is the third angle. The difference between these angles is then  $(100 - 2a)^\circ$ . Considering each option:
- A:  $100 - 2a = 0$  gives both  $a$  and  $100 - a$  to be 50. This triangle is therefore isosceles and not scalene.
- B:  $100 - 2a = 60$  gives  $a$  to be 20 and  $100 - a$  to be 80. This is again isosceles.
- Option D gives angles of 80, 0 and 100. Option E gives angles of 80,  $-10$  and 110. Neither of these cases forms a triangle.
- C:  $100 - 2a = 80$  gives  $a$  to be 10 and  $100 - a$  to be 90. All three angles are different so this is the correct option.