



17. Aaron has to choose a three-digit code for his bike lock. The digits can be chosen from 1 to 9. To help him remember them, Aaron chooses three different digits in increasing order, for example 278. How many such codes can be chosen?
- A 779                      B 504                      C 168                      D 84                      E 9

1687



©UKMT

- 
17. **D** One way to count the possible codes is in descending numerical order of the three-digit codes. The list begins: 789; 689, 679, 678; 589, 579, 578, 569, 568, 567; ... . Each initial digit  $n$  produces part of the list with the  $(8 - n)$ th triangular number of possible codes, where  $n \leq 7$ . The total number of possible codes is then the sum of these triangular numbers  $1 + 3 + 6 + 10 + 15 + 21 + 28$  including 1 code starting with the digit 7, all the way to 28 codes starting with the digit 1. The total number of codes that Aaron can choose is 84.