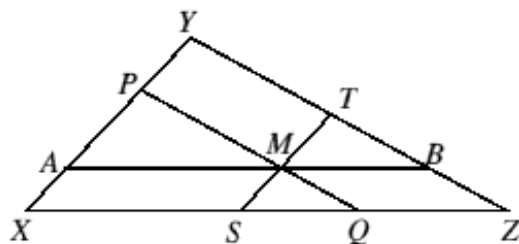




21. The diagram shows a triangle XYZ . The sides XY , YZ and XZ have lengths 2, 3 and 4 respectively. The lines AMB , PMQ and SMT are drawn parallel to the sides of triangle XYZ so that AP , QS and BT are of equal length. What is the length of AP ?



A $\frac{10}{11}$

B $\frac{11}{12}$

C $\frac{12}{13}$

D $\frac{13}{14}$

E $\frac{14}{15}$

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21. C All of the triangles in the diagram are similar as they contain the same angles. The sides of each triangle are therefore in the ratio 2 : 3 : 4. First consider triangle APM . Let $AP = x$, so that $AM = 2x$. Now considering triangle TBM , as $BT = x$, $BM = \frac{4x}{3}$. The quadrilateral $AMSX$ is a parallelogram as AM is parallel to XS and MS is parallel to AX . So $AM = XS = 2x$. Similarly $QZ = BM = \frac{4x}{3}$. Considering the base of triangle XYZ , $XS + SQ + QZ = 4$. So $2x + x + \frac{4x}{3} = 4$ and therefore $x = \frac{12}{13}$.