



18. What is the largest integer k whose square k^2 is a factor of $10!$?
[$10! = 10 \times 9 \times 8 \times 7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1.$]

A 6

B 256

C 360

D 720

E 5040

1588



©UKMT

-
18. D Expressed as a product of its prime factors, $10!$ is $2 \times 5 \times 3 \times 3 \times 2 \times 2 \times 2 \times 7 \times 2 \times 3 \times 5 \times 2 \times 2 \times 3 \times 2$ which is $2^8 \times 3^4 \times 5^2 \times 7$. This can be written as $(2^4 \times 3^2 \times 5)^2 \times 7$ so the largest integer k such that k^2 is a factor of $10!$ is $2^4 \times 3^2 \times 5$ which is 720.