



24. Which of the following is smallest?

- A  $10 - 3\sqrt{11}$     B  $8 - 3\sqrt{7}$     C  $5 - 2\sqrt{6}$     D  $9 - 4\sqrt{5}$     E  $7 - 4\sqrt{3}$

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24. A Each of the five expressions can be written in the form  $\sqrt{x} - \sqrt{x-1}$ , where  $x$  is in turn 100, 64, 25, 81 and 49. As  $(\sqrt{x} - \sqrt{x-1})(\sqrt{x} + \sqrt{x-1}) = x - (x-1) = 1$ , we can write  $(\sqrt{x} - \sqrt{x-1}) = \frac{1}{(\sqrt{x} + \sqrt{x-1})}$ . Since  $(\sqrt{x} + \sqrt{x-1})$  increases with  $x$ , then  $(\sqrt{x} - \sqrt{x-1})$  must decrease with  $x$ . Therefore, of the given expressions, the one corresponding to the largest value of  $x$  is the smallest. This is  $\sqrt{100} - \sqrt{99}$  which is  $10 - 3\sqrt{11}$ .