



22. A bag contains  $m$  blue and  $n$  yellow marbles. One marble is selected at random from the bag and its colour is noted. It is then returned to the bag along with  $k$  other marbles of the same colour. A second marble is now selected at random from the bag. What is the probability that the second marble is blue?

A  $\frac{m}{m+n}$       B  $\frac{n}{m+n}$       C  $\frac{m}{m+n+k}$       D  $\frac{m+k}{m+n+k}$       E  $\frac{m+n}{m+n+k}$

1492



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22. A The probability that the second marble is blue equals  $P(\text{2nd marble is blue given that the 1st marble is blue}) + P(\text{2nd marble is blue given that the 1st marble is yellow})$ , which is  $\frac{m}{m+n} \times \frac{m+k}{m+n+k} + \frac{n}{m+n} \times \frac{m}{m+n+k} = \frac{m^2 + mk + mn}{(m+n)(m+n+k)} = \frac{m(m+k+n)}{(m+n)(m+n+k)} = \frac{m}{m+n}$ .  
Note: this expression is independent of  $k$ .