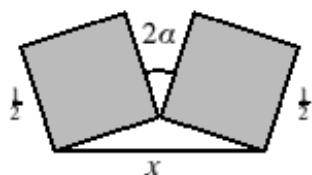




18. The diagram shows two squares, with sides of length $\frac{1}{2}$, inclined at an angle 2α to one another. What is the value of x ?

A $\cos \alpha$ B $\frac{1}{\cos \alpha}$ C $\sin \alpha$ D $\frac{1}{\sin \alpha}$ E $\tan \alpha$



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18. A In the diagram, D is the midpoint of AC . Triangle ABC is isosceles since $AB = BC = \frac{1}{2}$. Therefore, BD bisects $\angle ABC$ and BD is perpendicular to AC . The angles at a point total 360° , so $\angle ABC = 360^\circ - 2 \times 90^\circ - 2\alpha = 180^\circ - 2\alpha$. Therefore $\angle ABD = \angle CBD = 90^\circ - \alpha$. So $\angle BAD = \angle BCD = \alpha$.
Therefore $x = AC = 2 \times AD = 2 \times AB \cos \alpha = 2 \times \frac{1}{2} \cos \alpha = \cos \alpha$.

