



3. The robot *Lumber9* moves along the number line. *Lumber9* starts at 0, takes 1 step forward (to 1), then 2 steps backward (to  $-1$ ), then 3 steps forward, 4 steps backward, and so on, moving alternately forwards and backwards, one more step each time. At what number is *Lumber9* after 2011 steps?
- A 1006            B 27            C 11            D 0            E  $-18$

1173



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3. A After the  $n$ th step, *Lumber9* is at number: 
$$\begin{cases} \frac{n+1}{2} & \text{for } n \text{ odd,} \\ \frac{-n}{2} & \text{for } n \text{ even.} \end{cases}$$
- Hence when  $n = 2011$ , *Lumber9* is at number  $\frac{2011+1}{2} = 1006$ .