



17. Jamie conducted a survey on the food preferences of pupils at a school and discovered that 70% of the pupils like pears, 75% like oranges, 80% like bananas and 85% like apples. What is the smallest possible percentage of pupils who like all four of these fruits?
- A at least 10%      B at least 15%      C at least 20%  
D at least 25%      E at least 70%



- 
17. A Let  $a$ ,  $b$ ,  $o$  and  $p$  represent the percentage of pupils liking apples, bananas, oranges and pears respectively.  
As  $a = 85$ , there are 15% of pupils who do not like apples. As  $b = 80$ ,  $a \cap b$  is greater than or equal to  $80 - (100 - 85) = 65$ . As  $o = 75$ ,  $a \cap b \cap o$  is greater than or equal to  $75 - (100 - 65) = 40$ . Finally, as  $p = 70$ ,  $a \cap b \cap o \cap p$  is greater than or equal to  $70 - (100 - 40) = 10$ .  
Hence the percentage of pupils who like all four fruits is at least 10%.