



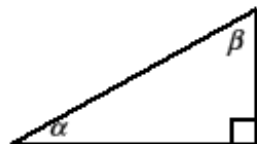
16. If  $\alpha < \beta$ , how many different values are there among the following expressions?

$$\sin \alpha \sin \beta$$

$$\sin \alpha \cos \beta$$

$$\cos \alpha \sin \beta$$

$$\cos \alpha \cos \beta$$



A 1

B 2

C 3

D 4

E It depends on the value of  $\alpha$

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16. C As  $\alpha + \beta = 90^\circ$ ,  $\sin \alpha = \cos \beta$ ;  $\cos \alpha = \sin \beta$ . So  $\sin \alpha \sin \beta = \sin \alpha \cos \alpha$ ;  $\sin \alpha \cos \beta = \sin^2 \alpha$ ;  $\cos \alpha \sin \beta = \cos^2 \alpha$ ;  $\cos \alpha \cos \beta = \cos \alpha \sin \alpha$ . As  $\alpha < \beta$ ,  $\alpha \neq 45^\circ$ . So  $\sin \alpha \neq \cos \alpha$ . Thus three of the four expressions have different values.