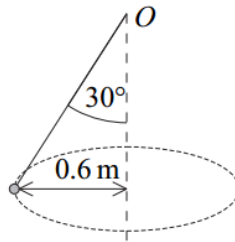


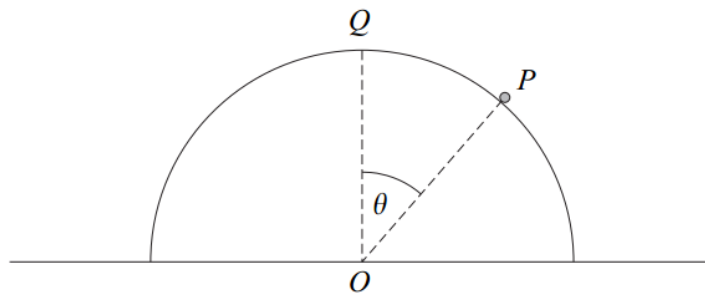
## Mechanics 2 Circular Motion

- 2 A particle, of mass 2 kg, is attached to one end of a light inextensible string. The other end is fixed to the point  $O$ . The particle is set into motion, so that it describes a horizontal circle of radius 0.6 metres, with the string at an angle of  $30^\circ$  to the vertical. The centre of the circle is vertically below  $O$ .



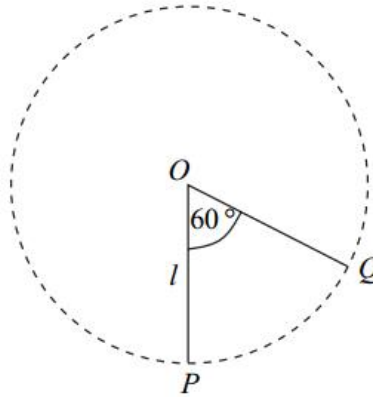
- (a) Show that the tension in the string is 22.6 N, correct to three significant figures. (3 marks)
- (b) Find the speed of the particle. (4 marks)
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- 7 A particle  $P$ , of mass  $m$  kg, is placed at the point  $Q$  on the top of a smooth upturned hemisphere of radius 3 metres and centre  $O$ . The plane face of the hemisphere is fixed to a horizontal table. The particle is set into motion with an initial horizontal velocity of  $2 \text{ m s}^{-1}$ . When the particle is on the surface of the hemisphere, the angle between  $OP$  and  $OQ$  is  $\theta$  and the particle has speed  $v \text{ m s}^{-1}$ .



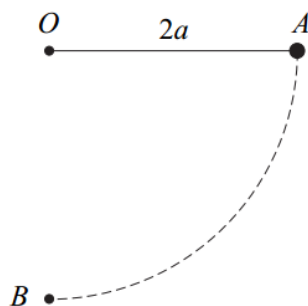
- (a) Show that  $v^2 = 4 + 6g(1 - \cos \theta)$ . (4 marks)
- (b) Find the value of  $\theta$  when the particle leaves the hemisphere. (5 marks)
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- 4 A particle of mass  $m$  is suspended from a fixed point  $O$  by a light inextensible string of length  $l$ . The particle hangs in equilibrium at the point  $P$  vertically below  $O$ . The particle is then set into motion with a horizontal velocity  $U$  so that it moves in a complete vertical circle with centre  $O$ . The point  $Q$  on the circle is such that  $\angle POQ = 60^\circ$ , as shown in the diagram.



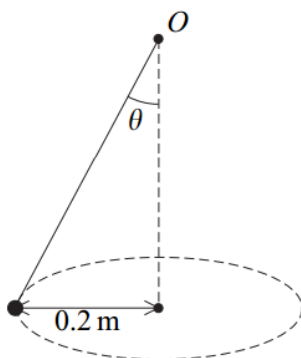
- (a) Find, in terms of  $g$ ,  $l$  and  $U$ , the speed of the particle at  $Q$ . (4 marks)
- (b) Find, in terms of  $g$ ,  $l$ ,  $m$  and  $U$ , the tension in the string when the particle is at  $Q$ . (5 marks)
- (c) Find, in terms of  $g$ ,  $l$ ,  $m$  and  $U$ , the tension in the string when the particle returns to  $P$ . (2 marks)
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- 6 A car of mass  $1200 \text{ kg}$  travels round a roundabout on a horizontal, circular path at a constant speed of  $14 \text{ m s}^{-1}$ . The radius of the circle is  $50 \text{ metres}$ . Assume that there is no resistance to the motion of the car and that the car can be modelled as a particle.
- (a) A friction force, directed towards the centre of the roundabout, acts on the car as it moves. Show that the magnitude of this friction force is  $4704 \text{ N}$ . (4 marks)
- (b) The coefficient of friction between the car and the road is  $\mu$ . Show that  $\mu \geq 0.4$ . (3 marks)
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- 3 A light inextensible string has length  $2a$ . One end of the string is attached to a fixed point  $O$  and a particle of mass  $m$  is attached to the other end. Initially, the particle is held at the point  $A$  with the string taut and horizontal. The particle is then released from rest and moves in a circular path. Subsequently, it passes through the point  $B$ , which is directly below  $O$ . The points  $O$ ,  $A$  and  $B$  are as shown in the diagram.



- (a) Show that the speed of the particle at  $B$  is  $2\sqrt{ag}$ . (3 marks)
- (b) Find the tension in the string as the particle passes through  $B$ . Give your answer in terms of  $m$  and  $g$ . (3 marks)
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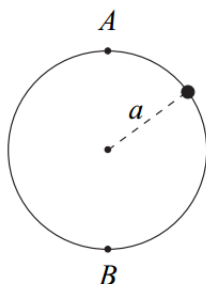
- 6 A particle is attached to one end of a light inextensible string. The other end of the string is attached to a fixed point  $O$ . The particle is set into motion, so that it describes a horizontal circle whose centre is vertically below  $O$ . The angle between the string and the vertical is  $\theta$ , as shown in the diagram.



- (a) The particle completes 40 revolutions every minute.
- Show that the angular speed of the particle is  $\frac{4\pi}{3}$  radians per second. (2 marks)
- (b) The radius of the circle is 0.2 metres.
- Find, in terms of  $\pi$ , the magnitude of the acceleration of the particle. (2 marks)

- (c) The mass of the particle is  $m$  kg and the tension in the string is  $T$  newtons.
- Draw a diagram showing the forces acting on the particle. (1 mark)
  - Explain why  $T \cos \theta = mg$ . (1 mark)
  - Find the value of  $\theta$ , giving your answer to the nearest degree. (5 marks)
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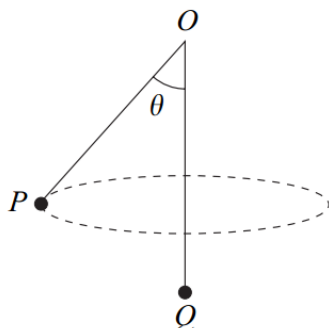
- 5 A bead of mass  $m$  moves on a smooth circular ring of radius  $a$  which is fixed in a vertical plane, as shown in the diagram. Its speed at  $A$ , the highest point of its path, is  $v$  and its speed at  $B$ , the lowest point of its path, is  $7v$ .



- Show that  $v = \sqrt{\frac{ag}{12}}$ . (5 marks)
  - Find the reaction of the ring on the bead, in terms of  $m$  and  $g$ , when the bead is at  $A$ . (4 marks)
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- 8 A particle,  $P$ , of mass 3 kg is attached to one end of a light inextensible string. The string passes through a smooth fixed ring,  $O$ , and a second particle,  $Q$ , of mass 5 kg is attached to the other end of the string. The particle  $Q$  hangs at rest vertically below the ring and the particle  $P$  moves with speed  $4 \text{ m s}^{-1}$  in a horizontal circle, as shown in the diagram.

The angle between  $OP$  and the vertical is  $\theta$ .



- Explain why the tension in the string is 49 N. (2 marks)
- Find  $\theta$ . (3 marks)
- Find the radius of the horizontal circle. (4 marks)