

## FP1 Conics Questions

8 A curve has equation  $y^2 = 12x$ .

(a) Sketch the curve. (2 marks)

(b) (i) The curve is translated by 2 units in the positive  $y$  direction. Write down the equation of the curve after this translation. (2 marks)

(ii) The **original** curve is reflected in the line  $y = x$ . Write down the equation of the curve after this reflection. (1 mark)

(c) (i) Show that if the straight line  $y = x + c$ , where  $c$  is a constant, intersects the curve  $y^2 = 12x$ , then the  $x$ -coordinates of the points of intersection satisfy the equation

$$x^2 + (2c - 12)x + c^2 = 0 \quad (3 \text{ marks})$$

(ii) Hence find the value of  $c$  for which the straight line is a tangent to the curve. (2 marks)

(iii) Using this value of  $c$ , find the coordinates of the point where the line touches the curve. (2 marks)

(iv) In the case where  $c = 4$ , determine whether the line intersects the curve or not. (3 marks)

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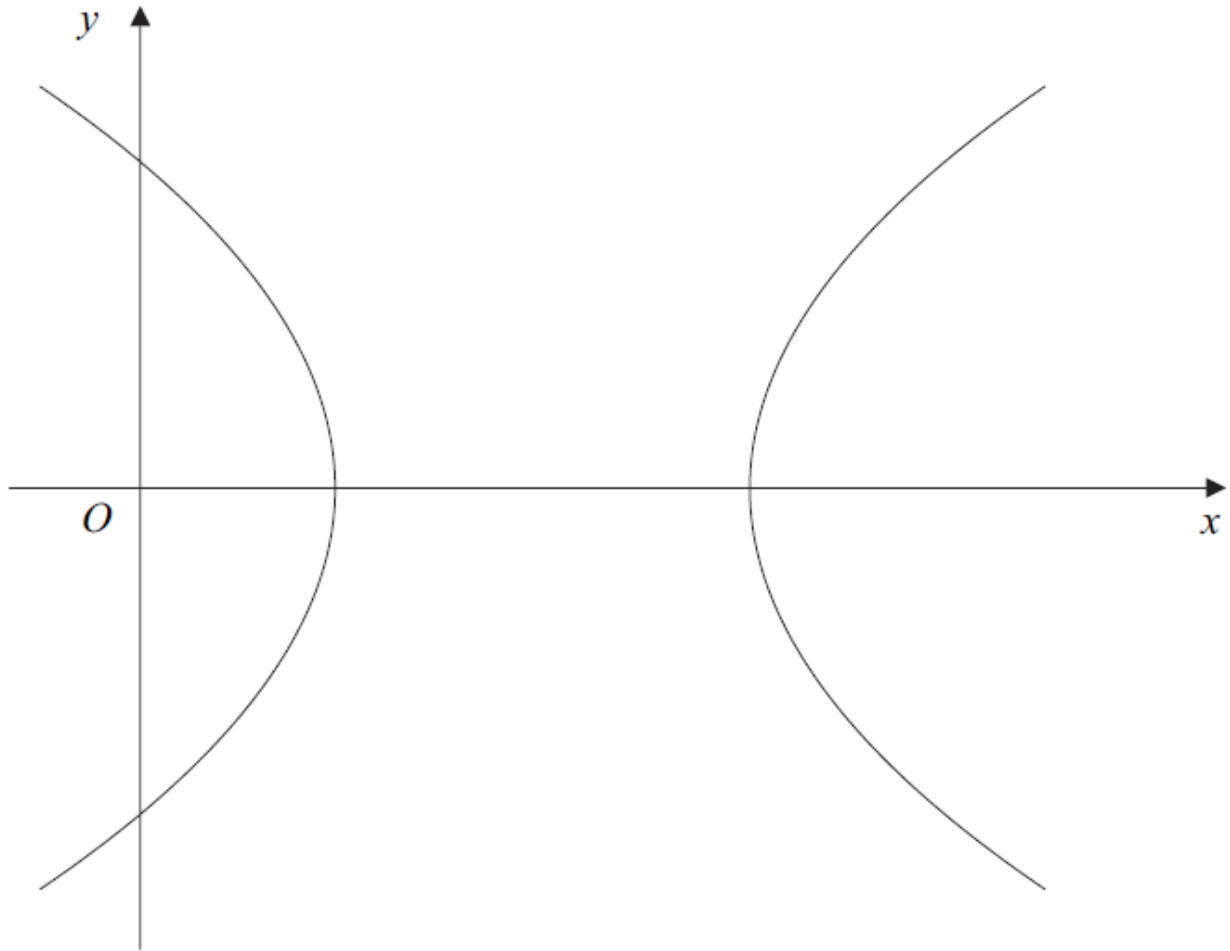
7 (a) Describe a geometrical transformation by which the hyperbola

$$x^2 - 4y^2 = 1$$

can be obtained from the hyperbola  $x^2 - y^2 = 1$ . (2 marks)

(b) The diagram shows the hyperbola  $H$  with equation

$$x^2 - y^2 - 4x + 3 = 0$$



By completing the square, describe a geometrical transformation by which the hyperbola  $H$  can be obtained from the hyperbola  $x^2 - y^2 = 1$ . (4 marks)

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8 A curve  $C$  has equation

$$\frac{x^2}{25} - \frac{y^2}{9} = 1$$

- (a) Find the  $y$ -coordinates of the points on  $C$  for which  $x = 10$ , giving each answer in the form  $k\sqrt{3}$ , where  $k$  is an integer. (3 marks)
- (b) Sketch the curve  $C$ , indicating the coordinates of any points where the curve intersects the coordinate axes. (3 marks)
- (c) Write down the equation of the tangent to  $C$  at the point where  $C$  intersects the positive  $x$ -axis. (1 mark)

- (d) (i) Show that, if the line  $y = x - 4$  intersects  $C$ , the  $x$ -coordinates of the points of intersection must satisfy the equation

$$16x^2 - 200x + 625 = 0 \quad (3 \text{ marks})$$

- (ii) Solve this equation and hence state the relationship between the line  $y = x - 4$  and the curve  $C$ . (2 marks)
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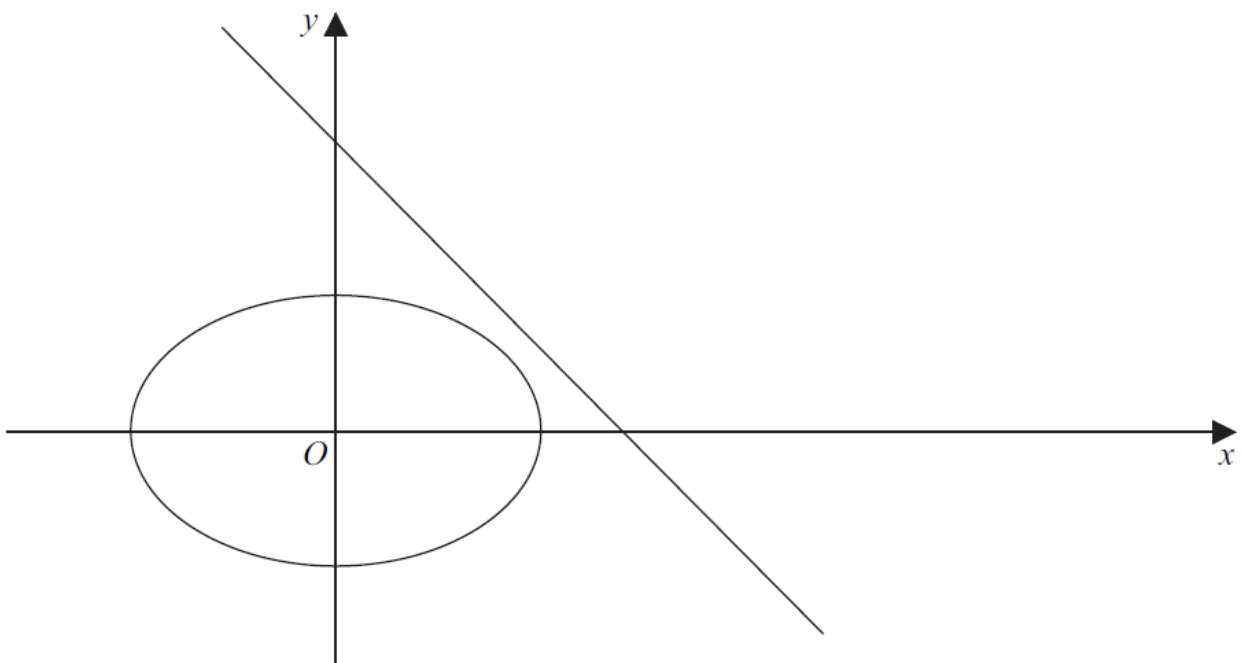
**9** [Figure 3, printed on the insert, is provided for use in this question.]

The diagram shows the curve with equation

$$\frac{x^2}{2} + y^2 = 1$$

and the straight line with equation

$$x + y = 2$$



- (a) Write down the exact coordinates of the points where the curve with equation  $\frac{x^2}{2} + y^2 = 1$  intersects the coordinate axes. (2 marks)
- (b) The curve is translated  $k$  units in the positive  $x$  direction, where  $k$  is a constant. Write down, in terms of  $k$ , the equation of the curve after this translation. (2 marks)
- (c) Show that, if the line  $x + y = 2$  intersects the **translated** curve, the  $x$ -coordinates of the points of intersection must satisfy the equation

$$3x^2 - 2(k + 4)x + (k^2 + 6) = 0 \quad (4 \text{ marks})$$

- (d) Hence find the two values of  $k$  for which the line  $x + y = 2$  is a tangent to the translated curve. Give your answer in the form  $p \pm \sqrt{q}$ , where  $p$  and  $q$  are integers. (4 marks)
- (e) On **Figure 3**, show the translated curves corresponding to these two values of  $k$ . (3 marks)
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