

FP1 Complex Number Questions

5 (a) (i) Calculate $(2 + i\sqrt{5})(\sqrt{5} - i)$. (3 marks)

(ii) Hence verify that $\sqrt{5} - i$ is a root of the equation

$$(2 + i\sqrt{5})z = 3z^*$$

where z^* is the conjugate of z . (2 marks)

(b) The quadratic equation

$$x^2 + px + q = 0$$

in which the coefficients p and q are real, has a complex root $\sqrt{5} - i$.

(i) Write down the other root of the equation. (1 mark)

6 It is given that $z = x + iy$, where x and y are real numbers.

(a) Write down, in terms of x and y , an expression for

$$(z + i)^*$$

where $(z + i)^*$ denotes the complex conjugate of $(z + i)$. (2 marks)

(b) Solve the equation

$$(z + i)^* = 2iz + 1$$

giving your answer in the form $a + bi$. (5 marks)

1 (a) Solve the following equations, giving each root in the form $a + bi$:

(i) $x^2 + 16 = 0$; (2 marks)

(ii) $x^2 - 2x + 17 = 0$. (2 marks)

(b) (i) Expand $(1 + x)^3$. (2 marks)

(ii) Express $(1 + i)^3$ in the form $a + bi$. (2 marks)

(iii) Hence, or otherwise, verify that $x = 1 + i$ satisfies the equation

$$x^3 + 2x - 4i = 0 (2 marks)$$

3 It is given that $z = x + iy$, where x and y are real numbers.

(a) Find, in terms of x and y , the real and imaginary parts of

$$z - 3iz^*$$

where z^* is the complex conjugate of z .

(3 marks)

(b) Find the complex number z such that

$$z - 3iz^* = 16$$

(3 marks)
