

## FP1 Complex Number Questions

5 (a) (i) Calculate  $(2 + i\sqrt{5})(\sqrt{5} - i)$ . (3 marks)

(ii) Hence verify that  $\sqrt{5} - i$  is a root of the equation

$$(2 + i\sqrt{5})z = 3z^*$$

where  $z^*$  is the conjugate of  $z$ . (2 marks)

(b) The quadratic equation

$$x^2 + px + q = 0$$

in which the coefficients  $p$  and  $q$  are real, has a complex root  $\sqrt{5} - i$ .

(i) Write down the other root of the equation. (1 mark)

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6 It is given that  $z = x + iy$ , where  $x$  and  $y$  are real numbers.

(a) Write down, in terms of  $x$  and  $y$ , an expression for

$$(z + i)^*$$

where  $(z + i)^*$  denotes the complex conjugate of  $(z + i)$ . (2 marks)

(b) Solve the equation

$$(z + i)^* = 2iz + 1$$

giving your answer in the form  $a + bi$ . (5 marks)

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1 (a) Solve the following equations, giving each root in the form  $a + bi$ :

(i)  $x^2 + 16 = 0$ ; (2 marks)

(ii)  $x^2 - 2x + 17 = 0$ . (2 marks)

(b) (i) Expand  $(1 + x)^3$ . (2 marks)

(ii) Express  $(1 + i)^3$  in the form  $a + bi$ . (2 marks)

(iii) Hence, or otherwise, verify that  $x = 1 + i$  satisfies the equation

$$x^3 + 2x - 4i = 0 (2 marks)$$

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3 It is given that  $z = x + iy$ , where  $x$  and  $y$  are real numbers.

(a) Find, in terms of  $x$  and  $y$ , the real and imaginary parts of

$$z - 3iz^*$$

where  $z^*$  is the complex conjugate of  $z$ .

*(3 marks)*

(b) Find the complex number  $z$  such that

$$z - 3iz^* = 16$$

*(3 marks)*

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